# CHURCHLANDS SENIOR HIGH SCHOOL
# Trial WACE Examination, 2011

**Question/Answer Booklet**

# MATHEMATICS 3C/3D
## Section One:
## Calculator-free

**Your name:**_____

**Student Number:** In figures | | | | | | | | |

In words _____

_____

**Circle your teacher:** HOY MENZIES KIROU SANDERS

## Time allowed for this section
Reading time before commencing work: five minutes
Working time for this section: fifty minutes

## Materials required/recommended for this section
***To be provided by the supervisor***
This Question/Answer Booklet
Formula Sheet

***To be provided by the candidate***
Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters

Special items: nil

## Important note to candidates

No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of exam |
|---|---|---|---|---|---|
| Section One: Calculator-free | 8 | 8 | 50 | 40 | 33 |
| Section Two: Calculator-assumed | 12 | 12 | 100 | 80 | 67 |
| | | | **Total** | 120 | 100 |

## Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2011*. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
   - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
   - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

3. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

4. It is recommended that you **do not use pencil**, except in diagrams.

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|---|---|---|---|---|---|
| Possible mark | 4 | 5 | 5 | 7 | 4 | 5 | 4 | 6 |
| Your mark | | | | | | | | |

**TOTAL:**

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**Section One: Calculator-free** **(40 Marks)**

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

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**Question 1** **(4 marks)**

Find the minimum and maximum values of $f(x) = 2x^3 - 3x^2 - 12x + 27$ over the interval $-3 \leq x \leq 3$.

**Question 2** **(5 marks)**

Find $\frac{dy}{dx}$ in terms of $x$ for each of the following.

(a) $y = x(1+2e^{3x})$ (2 marks)

(b) $y = \int_1^x t^2 + t - 1 \ dt$ (1 mark)

(c) $y = z^3 - z$ and $z = x^2 - 9$ (2 marks)

**Question 3** **(5 marks)**

Two independent events A and B are such that $P(A)=0.9$ and $P(B)=0.4$.

(a) Find $P(\overline{A \cup B})$. (2 marks)

(b) Find $P(\overline{B} \mid \overline{A} \cup B)$. (1 mark)

(c) Show that $\overline{A}$ and $\overline{B}$ are also independent. (2 marks)

**See next page**

**Question 4** **(7 marks)**

Two functions are defined as $f(x)=\sqrt{x-1}$ and $g(x)=\dfrac{1}{x-1}$.

(a) Evaluate $g \circ f\left(\dfrac{13}{9}\right)$. (2 marks)

(b) Find in simplified form $g \circ g(x)$. (2 marks)

(c) Determine the domain of $f(g(x))$. (3 marks)

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**Question 5** **(4 marks)**

Solve the system of equations

$$c + 2a = 3 + 4b$$
$$a + 2b + 2c = 4$$
$$5a + 3c = 5 + 2b$$

**See next page**

**Question 6** **(5 marks)**

(a) Determine $\int \frac{2e^{-0.2y}}{5}\,dy$. (1 mark)

(b) Determine $\int (t-1)\left(1-2t+t^2\right)^3\,dt$. (2 marks)

(c) Evaluate $\int_1^6 \frac{3}{x^2}\,dx$. (2 marks)

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**Question 7** **(4 marks)**

The region in the first quadrant bounded by $x=0$, $y=0$ and $y=1-\frac{x^2}{9}$ is rotated 360° about the $y$-axis. If $x$ and $y$ are distances measured in centimetres, find the volume of the solid formed.

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**Question 8** **(6 marks)**

The variables $k$ and $m$ are both integers such that $m^2 + 3 = 2k$.

(a) Use counter-examples to disprove any two of the three conjectures listed below. (2 marks)

- $m$ can be any even integer.

- $m$ can be any odd integer.

- $m$ must be a positive odd integer.

(b) Using the fact that any odd integer can be written in the form $2n + 1$ or otherwise, prove that $k$ is always the sum of three square numbers. (4 marks)

**End of questions**